metal-organic compounds

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Bis[3,3'-(piperazine-1,4-diyl)dipropanaminium] di- μ_2 -sulfido-bis[disulfidogermanate(IV)]

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Key indicators: single-crystal X-ray study; T = 296 K; mean σ (C–C) = 0.008 Å; R factor = 0.039; wR factor = 0.113; data-to-parameter ratio = 23.9.

In the title compound, $(C_{10}H_{26}N_4)_2[Ge_2S_6]$, the dimeric $[Ge_2S_6]^{4-}$ anion formed by two edge-sharing GeS₄ tetrahedral units lies around an inversion centre. The average terminal and bridging Ge-S bond lengths are 2.162 (7) and 2.267 (15) Å, respectively. The inorganic anions and organic cations are organized into a three-dimensional network by numerous N-H···S hydrogen bonds.

Related literature

For background to main group metal-chalcogenide compounds, see: Bedard *et al.* (1999); Nellis *et al.* (1995); Blachnik & Fehlker (2001); Zheng *et al.* (2002, 2005). For related structures, see: Jia *et al.* (2005); Xu *et al.* (2012).



Experimental

Crystal data

 $\begin{array}{l} ({\rm C}_{10}{\rm H}_{26}{\rm N}_4)_2[{\rm Ge}_2{\rm S}_6]\\ M_r=742.24\\ {\rm Monoclinic},\ P2_1/c\\ a=12.0111 \ (4) \ {\rm \AA}\\ b=7.7759 \ (3) \ {\rm \AA}\\ c=18.9777 \ (7) \ {\rm \AA}\\ \beta=103.569 \ (1)^\circ \end{array}$

 $V = 1722.99 (11) Å^{3}$ Z = 2Mo K\alpha radiation $\mu = 2.13 \text{ mm}^{-1}$ T = 296 K $0.38 \times 0.29 \times 0.16 \text{ mm}$

Data collection

Bruker APEXII CCD area-detector diffractometer Absorption correction: multi-scan (SADABS; Sheldrick, 1997) $T_{min} = 0.498, T_{max} = 0.727$

Refinement

$R[F^2 > 2\sigma(F^2)] = 0.039$	165 parameters
$wR(F^2) = 0.113$	H-atom parameters constrained
S = 1.07	$\Delta \rho_{\rm max} = 1.15 \text{ e } \text{\AA}^{-3}$
3950 reflections	$\Delta \rho_{\rm min} = -0.37 \ {\rm e} \ {\rm \AA}^{-3}$

16480 measured reflections

 $R_{\rm int} = 0.021$

3950 independent reflections

3194 reflections with $I > 2\sigma(I)$

Table 1 Hydrogen-bond geometry (Å, °).

$D - H \cdots A$	D-H	$H \cdot \cdot \cdot A$	$D \cdots A$	$D - \mathbf{H} \cdots A$
$N3-H3B\cdots S2^{i}$	0.89	2.48	3.278 (3)	149
N3−H3C···S3	0.89	2.34	3.225 (3)	170
$N3 - H3A \cdot \cdot \cdot S2^{ii}$	0.89	2.61	3.440 (3)	157
$N3-H3A\cdots S3^{ii}$	0.89	2.83	3.366 (3)	120
$N4 - H4C \cdot \cdot \cdot S2^{iii}$	0.89	2.53	3.408 (4)	169
$N4 - H4B \cdot \cdot \cdot S2^{iv}$	0.89	2.34	3.228 (4)	178
$N4 - H4A \cdots S3^{v}$	0.89	2.39	3.275 (4)	173

Symmetry codes: (i) x, y + 1, z; (ii) $-x + 1, y + \frac{1}{2}, -z + \frac{1}{2}$; (iii) x - 1, y, z; (iv) -x, -y, -z; (v) x - 1, y - 1, z.

Data collection: *APEX2* (Bruker, 2005); cell refinement: *SAINT* (Bruker, 2005); data reduction: *SAINT*; program(s) used to solve structure: *SHELXS97* (Sheldrick, 2008); program(s) used to refine structure: *SHELXL97* (Sheldrick, 2008); molecular graphics: *SHELXTL* (Sheldrick, 2008); software used to prepare material for publication: *SHELXTL*.

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Supplementary data and figures for this paper are available from the IUCr electronic archives (Reference: GK2485).

References

- Bedard, R. L., Wilson, S. T., Vail, L. D., Bennettand, J. M. & Flanigen, E. M. (1999). Zeolites: Facts, Figures, Future. Proceedings of the 8th International Zeolite Conference, edited by P. A. Jacobs & R. A. van Santen, p. 375. Amsterdam: Elsevier.
- Blachnik, R. & Fehlker, A. (2001). Z. Kristallogr. 216, 215-221.
- Bruker (2005). APEX2 and SAINT. Bruker AXS Inc., Madison, Wisconsin, USA.
- Jia, D.-X., Dai, J., Zhu, Q.-Y., Cao, L.-H. & Lin, H.-H. (2005). J. Solid State Chem. 178, 874-881.
- Nellis, D. M., Ko, Y., Tan, K., Koch, S. & Parise, J. (1995). J. Chem. Soc. Chem. Commun. pp. 541-542.
- Sheldrick, G. M. (1997). SADABS. University of Göttingen, Germany.
- Sheldrick, G. M. (2008). Acta Cryst. A64, 112-122.
- Xu, C., Zhang, J.-J., Duan, T., Chen, Q. & Zhang, Q.-F. (2012). Acta Cryst. E68, m154.
- Zheng, N., Bu, X. & Feng, P. (2005). Chem. Commun. pp. 2805-2806.
- Zheng, N., Bu, X., Wang, B. & Feng, P. (2002). Science, 298, 2366-2369.

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Bis[3,3'-(piperazine-1,4-diyl)dipropanaminium] di- μ_2 -sulfido-bis[disulfido-germanate(IV)]

Nian-Nian Wang, Chao Xu, Taike Duan, Qun Chen and Qian-Feng Zhang

S1. Comment

Since Bedard reported the first porous metal chalcogenide open framework in 1999 (Bedard *et al.*, 1999), a series of binary and ternary metal chalcogenide open-frameworks have been synthesized (Nellis *et al.*, 1995; Zheng *et al.*, 2005). Among the various synthetic methods, hydrothermal technique is the best choice for preparing related compounds due to gentle reaction conditions. Moreover, organic amines are often used as templates in the hydrothermal reactions. Therefore, amines with different structures play an important role for templating effect in the construction of open-frameworks (Zheng *et al.*, 2002). In this paper, we report the hydrothermal synthesis and crystal structure of an amine-templated thiogermanate, $[bappH_2]_2[Ge_2S_6]$ (bapp = 1,4-bis(3-aminopropyl)piperazine).

The title compound crystallizes in the monoclinic space group $P_{2_1/c}$ with a dimeric anion of $[Ge_2S_6]^4$ -located around inversion centre and with diprotonated 1,4-bis(3-aminopropyl)- piperazine in general position (Fig. 1). The dimeric $[Ge_2S_6]^4$ -anion is constructed by two edge-sharing tetrahedral GeS₄ units forming a planar Ge₂S₂ quadrilateral with the four terminal sulfur atoms lying on a perpendicular plane. The S—Ge—S angles in tetrahedral GeS₄ unit are in the ranges from 93.82 (3) to 114.12 (4)°. The average bond length of Ge—S_t (terminal bond) of 2.162 (7) Å is obviously shorter than that of Ge—S_b (bridging bond) [2.267 (15) Å]. The bond length values are similar to those found in the other thiogermanates (Jia *et al.* 2005; Xu *et al.*, 2012). The two terminal amine groups of 4-bis(3-aminopropyl)piperazine are protonated to balance negative charges of the dimeric anion. The [Ge₂S₆]⁴⁻ anions and [bappH₂]²⁺ cations are organized into an extended three-dimensional network by N—H···S hydrogen bonds (Fig. 2 and Table 1).

S2. Experimental

GeO₂ (104.6 mg, 1.0 mmol) and S powder (128.0 mg, 4.0 mmol) in the distilled water (4.8550 g) were mixed with 1,4bis(3-aminopropyl)piperazine (2.5640 g) in a 23 mL Teflon-lined stainless steel autoclave to and stirred for 20 min. The vessel was sealed and heated to 190°C for 6 d and then cooled to room temperature. Colorless flake crystals were obtained and air dried. The yield based on GeO₂ is about 45%. Analysis, calculated for $C_{20}H_{52}N_8S_6Ge_2$: C 32.4, H 7.06, N 15.1%; found C 32.2, H 6.98, N 14.8 %.

S3. Refinement

All C-bound H atoms were positioned geometrically and refined as riding atoms with C—H = 0.97 Å and $U_{iso}(H) = 1.2U_{eq}(C)$]. N-bound H atoms were located from a difference Fourier map but for final refinement they were were positioned geometrically with N—H = 0.89 Å and $U_{iso}(H) = 1.5U_{eq}(N)$].



Figure 1

The structure of the title compound, showing displacement ellipsoids at the 50% probability level. Atoms with the A label were generated by the symmetry operation -x+1, -y+1, -z.



Figure 2

Packing diagram of the title compound. Dashed lines donote hydrogen bonds.

Bis[3,3'-(piperazine-1,4-diyl)dipropanaminium] di-µ2-sulfido-bis[disulfidogermanate(IV)]

Crystal data

 $(C_{10}H_{26}N_{4})_{2}[Ge_{2}S_{6}]$ $M_{r} = 742.24$ Monoclinic, $P2_{1}/c$ Hall symbol: -P 2ybc a = 12.0111 (4) Å b = 7.7759 (3) Å c = 18.9777 (7) Å $\beta = 103.569$ (1)° V = 1722.99 (11) Å³ Z = 2

Data collection

Bruker APEXII CCD area-detector diffractometer Radiation source: fine-focus sealed tube Graphite monochromator phi and ω scans F(000) = 776 $D_x = 1.431 \text{ Mg m}^{-3}$ Mo K α radiation, $\lambda = 0.71073 \text{ Å}$ Cell parameters from 6783 reflections $\theta = 2.5-27.0^{\circ}$ $\mu = 2.13 \text{ mm}^{-1}$ T = 296 KBlock, colourless $0.38 \times 0.29 \times 0.16 \text{ mm}$

Absorption correction: multi-scan (*SADABS*; Sheldrick, 1997) $T_{min} = 0.498$, $T_{max} = 0.727$ 16480 measured reflections 3950 independent reflections 3194 reflections with $I > 2\sigma(I)$

$R_{\rm int} = 0.021$	$k = -10 \rightarrow 6$
$\theta_{\rm max} = 27.5^{\circ}, \theta_{\rm min} = 1.7^{\circ}$	$l = -22 \rightarrow 24$
$h = -15 \rightarrow 15$	

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Refinement on F^2	Secondary atom site location: difference Fourier
Least-squares matrix: full	map
$R[F^2 > 2\sigma(F^2)] = 0.039$	Hydrogen site location: inferred from
$wR(F^2) = 0.113$	neighbouring sites
S = 1.07	H-atom parameters constrained
3950 reflections	$w = 1/[\sigma^2(F_o^2) + (0.0586P)^2 + 1.3201P]$
165 parameters	where $P = (F_o^2 + 2F_c^2)/3$
0 restraints	$(\Delta/\sigma)_{\rm max} = 0.001$
Primary atom site location: structure-invariant	$\Delta ho_{ m max} = 1.15 \ m e \ m \AA^{-3}$
direct methods	$\Delta \rho_{\rm min} = -0.36 \text{ e } \text{\AA}^{-3}$

Special details

Geometry. All esds (except the esd in the dihedral angle between two l.s. planes) are estimated using the full covariance matrix. The cell esds are taken into account individually in the estimation of esds in distances, angles and torsion angles; correlations between esds in cell parameters are only used when they are defined by crystal symmetry. An approximate (isotropic) treatment of cell esds is used for estimating esds involving l.s. planes.

Refinement. Refinement of F^2 against ALL reflections. The weighted R-factor wR and goodness of fit S are based on F^2 , conventional R-factors R are based on F, with F set to zero for negative F^2 . The threshold expression of $F^2 > 2sigma(F^2)$ is used only for calculating R-factors(gt) etc. and is not relevant to the choice of reflections for refinement. R-factors based on F^2 are statistically about twice as large as those based on F, and R- factors based on ALL data will be even larger.

	x	У	Ζ	$U_{ m iso}$ */ $U_{ m eq}$
Gel	0.53261 (3)	0.44178 (4)	0.080248 (14)	0.04128 (12)
S1	0.38171 (8)	0.59109 (12)	0.01275 (4)	0.0541 (2)
S2	0.47606 (9)	0.19876 (11)	0.11556 (4)	0.0606 (3)
S3	0.63552 (8)	0.59389 (11)	0.16645 (4)	0.0565 (2)
N1	0.1088 (3)	0.4905 (5)	0.1532 (2)	0.0769 (10)
N2	-0.0300 (3)	0.1852 (5)	0.1210 (3)	0.1023 (15)
N3	0.4526 (3)	0.8528 (4)	0.20970 (15)	0.0630 (8)
H3A	0.4580	0.8401	0.2570	0.094*
H3B	0.4769	0.9572	0.2013	0.094*
H3C	0.4956	0.7738	0.1948	0.094*
N4	-0.3627 (4)	-0.0949 (5)	0.0505 (2)	0.0782 (10)
H4A	-0.3673	-0.1851	0.0785	0.117*
H4B	-0.3923	-0.1222	0.0043	0.117*
H4C	-0.4016	-0.0072	0.0630	0.117*
C6	0.1475 (5)	0.3408 (7)	0.1201 (5)	0.121 (2)
H6A	0.2301	0.3319	0.1362	0.145*
H6B	0.1284	0.3547	0.0679	0.145*
C7	0.0954 (5)	0.1827 (7)	0.1388 (5)	0.146 (3)
H7A	0.1227	0.1621	0.1903	0.175*
H7B	0.1207	0.0875	0.1134	0.175*
C8	-0.0710 (4)	0.3401 (7)	0.1474 (4)	0.0981 (16)
H8A	-0.0559	0.3348	0.1999	0.118*

Fractional atomic coordinates and isotropic or equivalent isotropic displacement parameters (\hat{A}^2)

H8B	-0.1532	0.3475	0.1288	0.118*
C9	-0.0168 (4)	0.4974 (6)	0.1262 (4)	0.0932 (15)
H9A	-0.0357	0.5077	0.0738	0.112*
H9B	-0.0466	0.5979	0.1459	0.112*
C10	0.1646 (4)	0.6473 (6)	0.1389 (3)	0.0880 (13)
H10A	0.1219	0.7451	0.1504	0.106*
H10B	0.1631	0.6528	0.0876	0.106*
C11	0.2881 (4)	0.6607 (6)	0.1822 (2)	0.0713 (10)
H11A	0.2915	0.6441	0.2334	0.086*
H4N	0.3338	0.5716	0.1669	0.086*
C12	0.3349 (4)	0.8321 (5)	0.1708 (2)	0.0725 (11)
H12A	0.3294	0.8485	0.1195	0.087*
H12B	0.2888	0.9201	0.1865	0.087*
C13	-0.0732 (7)	0.0324 (9)	0.1558 (5)	0.151 (3)
H13A	-0.0359	-0.0697	0.1430	0.182*
H13B	-0.0489	0.0458	0.2079	0.182*
C14	-0.1959 (7)	0.0022 (10)	0.1373 (3)	0.129 (3)
H14A	-0.2341	0.1056	0.1479	0.155*
H14B	-0.2130	-0.0889	0.1680	0.155*
C15	-0.2442 (5)	-0.0463 (8)	0.0594 (3)	0.1042 (18)
H15A	-0.2385	0.0503	0.0281	0.125*
H15B	-0.2012	-0.1416	0.0461	0.125*

Atomic displacement parameters $(Å^2)$

	U^{11}	U^{22}	U^{33}	U^{12}	U^{13}	U^{23}
Ge1	0.0602 (2)	0.03395 (18)	0.02960 (17)	0.00094 (13)	0.01036 (13)	0.00344 (11)
S 1	0.0626 (5)	0.0634 (5)	0.0388 (4)	0.0157 (4)	0.0166 (3)	0.0086 (3)
S2	0.0973 (7)	0.0428 (4)	0.0406 (4)	-0.0147 (4)	0.0140 (4)	0.0072 (3)
S3	0.0768 (6)	0.0487 (5)	0.0396 (4)	-0.0091 (4)	0.0046 (4)	-0.0021 (3)
N1	0.066 (2)	0.0546 (18)	0.111 (3)	0.0014 (16)	0.0225 (19)	-0.0006 (19)
N2	0.076 (2)	0.062 (2)	0.152 (4)	-0.0009 (19)	-0.008(3)	-0.010 (3)
N3	0.099 (2)	0.0472 (16)	0.0448 (15)	-0.0004 (16)	0.0211 (15)	-0.0012 (12)
N4	0.102 (3)	0.068 (2)	0.066 (2)	-0.0073 (19)	0.0226 (19)	-0.0058 (17)
C6	0.077 (3)	0.074 (3)	0.216 (7)	0.006 (3)	0.040 (4)	-0.035 (4)
C7	0.078 (3)	0.062 (3)	0.271 (10)	0.010 (3)	-0.014 (5)	-0.027 (4)
C8	0.068 (3)	0.083 (3)	0.138 (5)	-0.008(2)	0.012 (3)	-0.011 (3)
C9	0.073 (3)	0.066 (3)	0.136 (5)	0.013 (2)	0.014 (3)	0.002 (3)
C10	0.088 (3)	0.068 (3)	0.109 (4)	0.005 (2)	0.026 (3)	0.013 (3)
C11	0.074 (2)	0.075 (3)	0.066 (2)	0.000 (2)	0.0193 (19)	-0.001 (2)
C12	0.101 (3)	0.058 (2)	0.056 (2)	0.014 (2)	0.014 (2)	-0.0031 (18)
C13	0.147 (6)	0.091 (4)	0.185 (8)	-0.047 (4)	-0.022 (6)	0.026 (5)
C14	0.157 (6)	0.136 (5)	0.086 (4)	-0.068 (5)	0.012 (4)	0.015 (4)
C15	0.107 (4)	0.128 (5)	0.079 (3)	-0.018 (3)	0.025 (3)	0.004 (3)

Geometric parameters (Å, °)

Gel—S3	2.1573 (9)	C7—H7B	0.9700	
Ge1—S2	2.1669 (9)	C8—C9	1.485 (7)	
Ge1—S1	2.2770 (9)	C8—H8A	0.9700	
S1—Ge1 ⁱ	2.2564 (8)	C8—H8B	0.9700	
N1-C10	1.448 (6)	С9—Н9А	0.9700	
N1C6	1.450 (6)	С9—Н9В	0.9700	
N1—C9	1.476 (6)	C10—C11	1.522 (6)	
N2—C8	1.435 (7)	C10—H10A	0.9700	
N2—C7	1.465 (7)	C10—H10B	0.9700	
N2-C13	1.509 (8)	C11—C12	1.482 (6)	
N3—C12	1.442 (5)	C11—H11A	0.9700	
N3—H3A	0.8900	C11—H4N	0.9700	
N3—H3B	0.8900	C12—H12A	0.9700	
N3—H3C	0.8900	C12—H12B	0.9700	
N4—C15	1.443 (7)	C13—C14	1.451 (10)	
N4—H4A	0.8900	C13—H13A	0.9700	
N4—H4B	0.8900	C13—H13B	0.9700	
N4—H4C	0.8900	C14—C15	1.504 (8)	
С6—С7	1.460 (8)	C14—H14A	0.9700	
С6—Н6А	0.9700	C14—H14B	0.9700	
С6—Н6В	0.9700	C15—H15A	0.9700	
С7—Н7А	0.9700	C15—H15B	0.9700	
S3—Ge1—S2	114.15 (3)	N1—C9—C8	110.6 (4)	
S3—Ge1—S1 ⁱ	111.71 (4)	N1—C9—H9A	109.5	
S2—Ge1—S1 ⁱ	112.13 (4)	С8—С9—Н9А	109.5	
S3—Ge1—S1	112.70 (4)	N1—C9—H9B	109.5	
S2—Ge1—S1	110.66 (4)	С8—С9—Н9В	109.5	
S1 ⁱ —Ge1—S1	93.82 (3)	H9A—C9—H9B	108.1	
Gel ⁱ —S1—Gel	86.18 (3)	N1-C10-C11	113.1 (4)	
C10-N1-C6	112.7 (4)	N1-C10-H10A	109.0	
C10—N1—C9	112.6 (4)	C11-C10-H10A	109.0	
C6—N1—C9	106.5 (4)	N1-C10-H10B	109.0	
C8—N2—C7	110.4 (4)	C11—C10—H10B	109.0	
C8—N2—C13	109.1 (6)	H10A—C10—H10B	107.8	
C7—N2—C13	109.2 (5)	C12—C11—C10	109.7 (4)	
C12—N3—H3A	109.5	C12—C11—H11A	109.7	
C12—N3—H3B	109.5	C10—C11—H11A	109.7	
H3A—N3—H3B	109.5	C12—C11—H4N	109.7	
C12—N3—H3C	109.5	C10—C11—H4N	109.7	
H3A—N3—H3C	109.5	H11A—C11—H4N	108.2	
H3B—N3—H3C	109.5	N3—C12—C11	112.7 (3)	
C15—N4—H4A	109.5	N3—C12—H12A	109.1	
C15—N4—H4B	109.5	C11—C12—H12A	109.1	
H4A—N4—H4B	109.5	N3—C12—H12B	109.1	
C15—N4—H4C	109.5	C11—C12—H12B	109.1	

H4A—N4—H4C	109.5	H12A—C12—H12B	107.8
H4B—N4—H4C	109.5	C14—C13—N2	117.1 (6)
N1—C6—C7	111.8 (5)	C14—C13—H13A	108.0
N1—C6—H6A	109.3	N2—C13—H13A	108.0
С7—С6—Н6А	109.3	C14—C13—H13B	108.0
N1—C6—H6B	109.3	N2—C13—H13B	108.0
С7—С6—Н6В	109.3	H13A—C13—H13B	107.3
H6A—C6—H6B	107.9	C13—C14—C15	114.5 (7)
C6—C7—N2	114.2 (5)	C13—C14—H14A	108.6
С6—С7—Н7А	108.7	C15—C14—H14A	108.6
N2—C7—H7A	108.7	C13—C14—H14B	108.6
С6—С7—Н7В	108.7	C15—C14—H14B	108.6
N2—C7—H7B	108.7	H14A—C14—H14B	107.6
H7A—C7—H7B	107.6	N4—C15—C14	108.9 (5)
N2—C8—C9	112.9 (5)	N4—C15—H15A	109.9
N2—C8—H8A	109.0	C14—C15—H15A	109.9
С9—С8—Н8А	109.0	N4—C15—H15B	109.9
N2—C8—H8B	109.0	C14—C15—H15B	109.9
С9—С8—Н8В	109.0	H15A—C15—H15B	108.3
H8A—C8—H8B	107.8		

Symmetry code: (i) -x+1, -y+1, -z.

Hydrogen-bond geometry (Å, °)

D—H···A	D—H	H···A	D···A	<i>D</i> —H··· <i>A</i>
N3—H3 <i>B</i> ···S2 ⁱⁱ	0.89	2.48	3.278 (3)	149
N3—H3 <i>C</i> ···S3	0.89	2.34	3.225 (3)	170
N3—H3A···S2 ⁱⁱⁱ	0.89	2.61	3.440 (3)	157
N3—H3A···S3 ⁱⁱⁱ	0.89	2.83	3.366 (3)	120
N4— $H4C$ ···S2 ^{iv}	0.89	2.53	3.408 (4)	169
N4—H4 B ···S2 ^v	0.89	2.34	3.228 (4)	178
N4—H4A····S3 ^{vi}	0.89	2.39	3.275 (4)	173

Symmetry codes: (ii) *x*, *y*+1, *z*; (iii) –*x*+1, *y*+1/2, –*z*+1/2; (iv) *x*–1, *y*, *z*; (v) –*x*, –*y*, –*z*; (vi) *x*–1, *y*–1, *z*.