

Redetermination of dicerium(III) tris(sulfate) tetrahydrate

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Key indicators: single-crystal X-ray study; $T = 293$ K; mean $\sigma(\text{Ce}-\text{O}) = 0.003$ Å; R factor = 0.027; wR factor = 0.067; data-to-parameter ratio = 10.2.

$\text{Ce}_2(\text{SO}_4)_3(\text{H}_2\text{O})_4$ was obtained hydrothermally from an aqueous solution of cerium(III) oxide, trimethylamine and sulfuric acid. The precision of the structure determination has been significantly improved compared with the previous result [Dereigne (1972). *Bull. Soc. Fr. Mineral. Cristallogr.* **95**, 269–280]. The coordination about the two Ce atoms is achieved by seven and six bridging O atoms from sulfate anions. Each S atom makes four S—O—Ce linkages through bridging O atoms. The coordination sphere of each Ce is completed by two water molecules, which act as terminal ligands.

Related literature

For related literature, see: Doran *et al.* (2002); Li *et al.* (1998); Plévert *et al.* (2001); Shi (1987); Xu, Cheng & You (2006); Xu, Ding *et al.* (2006); Yuan *et al.* (2004); Zhang *et al.* (2004). For the previous structure determination, see: Dereigne (1972).

Experimental

Crystal data

$\text{Ce}_2(\text{SO}_4)_3(\text{H}_2\text{O})_4$	$V = 1272.5$ (2) Å ³
$M_r = 640.48$	$Z = 4$
Monoclinic, $P2_1/n$	Mo $K\alpha$ radiation
$a = 13.1257$ (14) Å	$\mu = 7.65$ mm ⁻¹
$b = 7.2520$ (8) Å	$T = 293$ (2) K
$c = 13.3823$ (14) Å	$0.13 \times 0.12 \times 0.10$ mm
$\beta = 92.5720$ (10)°	

Data collection

Bruker APEX2 CCD diffractometer	5923 measured reflections
Absorption correction: multi-scan (SADABS; Sheldrick, 2003)	2201 independent reflections
$T_{\min} = 0.437$, $T_{\max} = 0.515$ (expected range = 0.394–0.466)	2071 reflections with $I > 2\sigma(I)$
	$R_{\text{int}} = 0.032$

Refinement

$R[F^2 > 2\sigma(F^2)] = 0.027$	16 restraints
$wR(F^2) = 0.067$	Only H-atom coordinates refined
$S = 1.09$	$\Delta\rho_{\text{max}} = 1.12$ e Å ⁻³
2201 reflections	$\Delta\rho_{\text{min}} = -2.16$ e Å ⁻³
215 parameters	

Table 1

Selected geometric parameters (Å, °).

Ce1—O10	2.449 (2)	Ce2—O1 ⁱⁱⁱ	2.354 (3)
Ce1—O7	2.465 (3)	Ce2—O4 ^{iv}	2.430 (3)
Ce1—O12 ⁱ	2.476 (4)	Ce2—O5 ⁱⁱⁱ	2.470 (3)
Ce1—O11 ⁱⁱ	2.517 (3)	Ce2—O6 ^v	2.489 (3)
Ce1—O4 ^w	2.524 (3)	Ce2—O3 ^w	2.494 (3)
Ce1—O3	2.547 (3)	Ce2—O2 ^w	2.497 (3)
Ce1—O3 ^t	2.621 (3)	Ce2—O9	2.529 (4)
Ce1—O1 ^w	2.647 (3)	Ce2—O8	2.659 (3)
Ce1—O11	2.710 (3)		
O10—Ce1—O3	150.11 (9)	O3—Ce1—O11	53.24 (9)

Symmetry codes: (i) $-x + 1, -y, -z + 2$; (ii) $-x + 1, -y + 1, -z + 2$; (iii) $x - \frac{1}{2}, -y + \frac{1}{2}, z - \frac{1}{2}$; (iv) $-x, -y, -z + 2$; (v) $-x, -y + 1, -z + 2$.

Data collection: APEX2 (Bruker, 2005); cell refinement: SAINT (Bruker, 2005); data reduction: SAINT; program(s) used to solve structure: SHELXS97 (Sheldrick, 1997a); program(s) used to refine structure: SHELXL97 (Sheldrick, 1997a); molecular graphics: SHELXTL (Sheldrick, 1997b); software used to prepare material for publication: SHELXTL.

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Supplementary data and figures for this paper are available from the IUCr electronic archives (Reference: FI2049).

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supporting information

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S1. Comment

Over the past decades, the design and synthesis of new three-dimensional solid state materials have received great attention, due to their functional applications in catalysis and optical device. As the building elements germanium has been chosen to synthesize new porous materials (Li *et al.*, 1998; Plévert *et al.*, 2001; Xu, Cheng & You, 2006; Xu, Ding *et al.*, 2006). In the last few years, an important advance in three dimensional inorganic materials has been achieved by study of lanthanide sulfates frameworks (Zhang *et al.*, 2004; Yuan *et al.*, 2004; Xu, Ding *et al.*, 2006; Doran *et al.*, 2002). In this work, we synthesized the title compound, Cerium(3+) sulfate tetrahydrate, which features a three-dimensional framework. The structure of title compound had been reported previously (Dereigne *et al.*, 1972), however, the precision of redetermination is much improved.

As isostructure with $\text{La}_2(\text{SO}_4)_3(\text{H}_2\text{O})_4$ and $\text{Nd}_2(\text{SO}_4)_3(\text{H}_2\text{O})_4$ (Shi, 1987), the framework of title compound is constructed from CeO_9 and CeO_8 polyhedra and SO_4 tetrahedra. As shown in Fig. 1 and 2, the asymmetric unit contains two Ce^{3+} , three SO_4^{2-} groups and four water molecules, all of which belong to the inorganic framework. The coordination about Ce1 and Ce2, respectively, is achieved by bridging oxygen atoms from sulfate anions. Each S atom makes four S–O–Ce linkages through bridging O atoms. The coordination sphere of each Ce is completed by two water molecules, which act as terminal ligands of Ce^{3+} .

The Ce atom has the typical geometrical parameters, with Ce–O distances of 2.354 (3)–2.710 (3) Å (Table 1). The O–Ce–O angles are between 59.28 (14) and 139.03 (14)°. These bond distances and bond angles are in agreement with those found in similar rare-earth compounds (Zhang *et al.*, 2004; Yuan *et al.*, 2004). The geometry of the sulfate ions is unexceptional. Fig. 3 shows the three-dimensional arrangement in the unit cell, displaying the way the different CeO_9 polyhedra are connected by bridging sulfates.

S2. Experimental

Colorless block-shaped crystals were synthesized hydrothermally from a mixture of $\text{CeCl}_3 \cdot 6\text{H}_2\text{O}$, H_2SO_4 (98%), H_2O and trimethylamine (25%). All the chemicals are purchased from Shanghai Chemical Reagent Factory. In a typical synthesis, $\text{CeCl}_3 \cdot 6\text{H}_2\text{O}$ (0.2993 g) was dissolved in a mixture of trimethylamine (25%, 0.7893 g) and of water (1 ml) followed by the addition of H_2SO_4 (98%) (0.3528 g) with constant stirring. Finally, the mixture was kept in a 25 ml Teflon-lined steel autoclave at 180 °C for 6 days. The autoclave was slowly cooled to room temperature, and then the product was filtered, washed with distilled water, and dried at room temperature. Colorless block-shaped crystals of the title compound were obtained.

S3. Refinement

The highest peak in the difference map is 1.12 e/Å³, and 1.26 (2) Å from Ce₂, while the minimum peak is -2.16 (2) Å from Ce₁. 5. The H atoms of water were located from different map, and the O–H distances are restrained to 0.85 (2) Å.

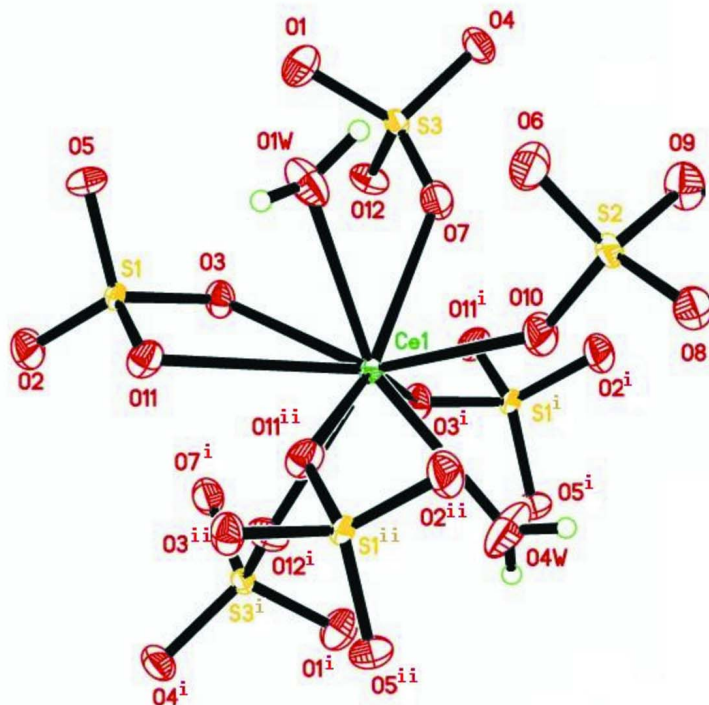


Figure 1

The coordination of Ce1 for title compound. Displacement ellipsoids at the 70% probability level. Symmetry codes as in Table 1.

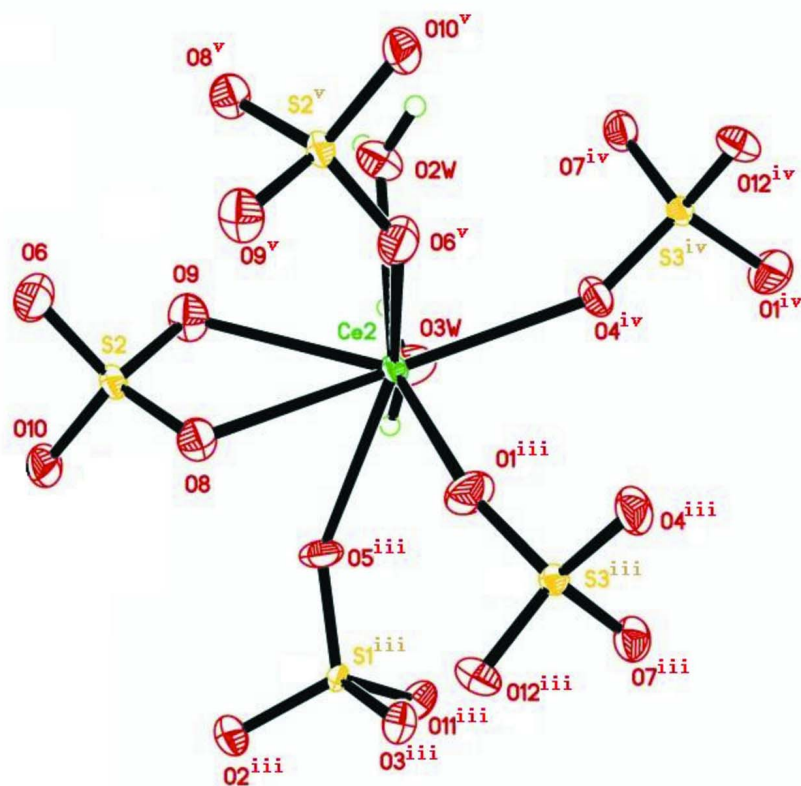


Figure 2

The coordination of Ce2 for title compound. Displacement ellipsoids at the 70% probability level. Symmetry codes as in Table 1.

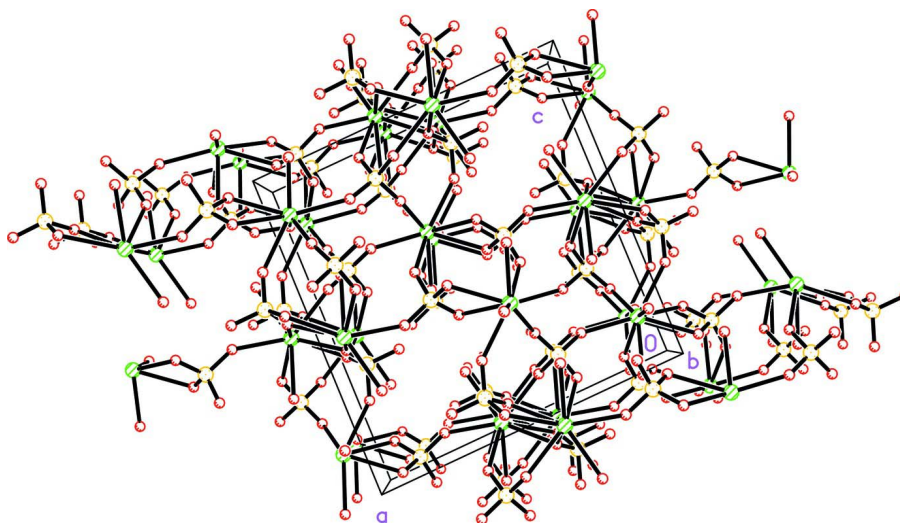


Figure 3

The crystal packing in the unit cell of $\text{Ce}(\text{SO}_4)(\text{OH})$.

dicerium(III) tris(sulfate) tetrahydrate

Crystal data

Ce₂(SO₄)₃(H₂O)₄
M_r = 640.48
 Monoclinic, *P*2₁/*n*
 Hall symbol: -*P* 2₁*n*
a = 13.1257 (14) Å
b = 7.2520 (8) Å
c = 13.3823 (14) Å
 β = 92.572 (1)°
V = 1272.5 (2) Å³
Z = 4

F(000) = 1200
D_x = 3.343 Mg m⁻³
 Mo *K*α radiation, λ = 0.71073 Å
 Cell parameters from 2201 reflections
 θ = 2.1–25.0°
 μ = 7.65 mm⁻¹
T = 293 K
 Block, colourless
 0.13 × 0.12 × 0.10 mm

Data collection

Bruker APEX2 CCD
 diffractometer
 Radiation source: fine-focus sealed tube
 Graphite monochromator
 ω scans
 Absorption correction: multi-scan
 (*SADABS*; Sheldrick, 2003)
T_{min} = 0.437, *T_{max}* = 0.515

5923 measured reflections
 2201 independent reflections
 2071 reflections with *I* > 2σ(*I*)
R_{int} = 0.032
 θ_{\max} = 25.0°, θ_{\min} = 2.1°
h = -12→15
k = -8→8
l = -15→12

Refinement

Refinement on *F*²
 Least-squares matrix: full
R[*F*² > 2σ(*F*²)] = 0.027
wR(*F*²) = 0.067
S = 1.09
 2201 reflections
 215 parameters
 16 restraints
 Primary atom site location: structure-invariant
 direct methods
 Secondary atom site location: difference Fourier
 map

Hydrogen site location: inferred from
 neighbouring sites
 Only H-atom coordinates refined
 $w = 1/[\sigma^2(F_o^2) + (0.0371P)^2 + 1.0649P]$
 where $P = (F_o^2 + 2F_c^2)/3$
 $(\Delta/\sigma)_{\max} = 0.001$
 $\Delta\rho_{\max} = 1.12 \text{ e \AA}^{-3}$
 $\Delta\rho_{\min} = -2.16 \text{ e \AA}^{-3}$
 Extinction correction: *SHELXL*,
 $F_c^* = kF_c[1 + 0.001x F_c^2 \lambda^3 / \sin(2\theta)]^{-1/4}$
 Extinction coefficient: 0.0953 (15)

Special details

Geometry. All e.s.d.'s (except the e.s.d. in the dihedral angle between two l.s. planes) are estimated using the full covariance matrix. The cell e.s.d.'s are taken into account individually in the estimation of e.s.d.'s in distances, angles and torsion angles; correlations between e.s.d.'s in cell parameters are only used when they are defined by crystal symmetry. An approximate (isotropic) treatment of cell e.s.d.'s is used for estimating e.s.d.'s involving l.s. planes.

Refinement. Refinement of *F*² against ALL reflections. The weighted *R*-factor *wR* and goodness of fit *S* are based on *F*², conventional *R*-factors *R* are based on *F*, with *F* set to zero for negative *F*². The threshold expression of *F*² > σ(*F*²) is used only for calculating *R*-factors(gt) *etc.* and is not relevant to the choice of reflections for refinement. *R*-factors based on *F*² are statistically about twice as large as those based on *F*, and *R*-factors based on ALL data will be even larger.

Fractional atomic coordinates and isotropic or equivalent isotropic displacement parameters (Å²)

	<i>x</i>	<i>y</i>	<i>z</i>	<i>U_{iso}</i> [*] / <i>U_{eq}</i>
Ce1	0.413692 (17)	0.24066 (3)	0.964316 (18)	0.00669 (14)
Ce2	-0.073660 (17)	0.26197 (3)	0.849355 (18)	0.00793 (14)
S1	0.59971 (8)	0.26189 (10)	1.13380 (8)	0.0068 (2)

S2	0.13846 (6)	0.38957 (12)	0.95722 (7)	0.0088 (2)
S3	0.34712 (6)	-0.10740 (12)	1.15208 (7)	0.0077 (2)
O1	0.3887 (2)	-0.0086 (4)	1.2394 (2)	0.0179 (6)
O2	0.7082 (2)	0.2370 (3)	1.1325 (3)	0.0164 (7)
O3	0.54510 (19)	0.0990 (3)	1.0873 (2)	0.0109 (6)
O4	0.2552 (2)	-0.2061 (4)	1.1792 (2)	0.0153 (6)
O5	0.5660 (2)	0.2917 (4)	1.2352 (2)	0.0152 (6)
O6	0.15247 (19)	0.4888 (4)	1.0522 (2)	0.0174 (6)
O7	0.32350 (19)	0.0207 (4)	1.0695 (2)	0.0137 (6)
O8	0.07908 (19)	0.4978 (4)	0.8833 (2)	0.0134 (6)
O9	0.0762 (3)	0.2206 (4)	0.9727 (3)	0.0158 (7)
O10	0.23802 (19)	0.3357 (4)	0.9218 (2)	0.0163 (6)
O11	0.5637 (2)	0.4210 (4)	1.0702 (2)	0.0121 (6)
O12	0.4231 (3)	-0.2449 (3)	1.1215 (3)	0.0134 (7)
O1W	0.3582 (2)	0.3879 (4)	1.1345 (2)	0.0181 (6)
H1WB	0.2964 (19)	0.371 (5)	1.152 (4)	0.027*
H1WA	0.381 (3)	0.497 (4)	1.138 (4)	0.027*
O2W	-0.13163 (19)	0.1354 (4)	1.0108 (2)	0.0155 (6)
H2WB	-0.185 (2)	0.179 (5)	1.037 (3)	0.023*
H2WA	-0.114 (3)	0.028 (4)	1.030 (3)	0.023*
O3W	-0.0481 (2)	-0.0777 (4)	0.8356 (2)	0.0218 (6)
H3WB	-0.049 (3)	-0.142 (4)	0.889 (2)	0.033*
H3WA	-0.005 (3)	-0.115 (4)	0.793 (3)	0.033*
O4W	0.3708 (3)	0.2180 (5)	0.7790 (3)	0.0245 (8)
H4WB	0.401 (3)	0.147 (6)	0.738 (3)	0.037*
H4WA	0.312 (2)	0.258 (6)	0.758 (4)	0.037*

Atomic displacement parameters (\AA^2)

	U^{11}	U^{22}	U^{33}	U^{12}	U^{13}	U^{23}
Ce1	0.0052 (2)	0.00827 (18)	0.0066 (2)	0.00028 (6)	-0.00017 (12)	0.00084 (7)
Ce2	0.0056 (2)	0.00981 (18)	0.0083 (2)	0.00046 (6)	0.00028 (13)	0.00215 (7)
S1	0.0057 (5)	0.0090 (5)	0.0055 (5)	0.0001 (3)	-0.0013 (4)	0.0004 (3)
S2	0.0057 (4)	0.0099 (4)	0.0106 (5)	0.0002 (3)	-0.0002 (3)	-0.0003 (3)
S3	0.0062 (4)	0.0089 (4)	0.0082 (5)	-0.0012 (3)	0.0006 (3)	-0.0009 (3)
O1	0.0210 (14)	0.0193 (14)	0.0134 (14)	-0.0032 (12)	-0.0009 (11)	-0.0063 (12)
O2	0.0081 (16)	0.0242 (17)	0.0169 (18)	0.0004 (10)	0.0000 (13)	-0.0027 (10)
O3	0.0113 (13)	0.0083 (13)	0.0129 (14)	-0.0018 (10)	-0.0022 (11)	0.0008 (11)
O4	0.0084 (14)	0.0212 (13)	0.0164 (15)	-0.0026 (12)	0.0005 (11)	0.0046 (13)
O5	0.0160 (16)	0.0219 (13)	0.0081 (15)	-0.0015 (12)	0.0039 (12)	-0.0029 (13)
O6	0.0148 (14)	0.0217 (14)	0.0153 (14)	0.0032 (11)	-0.0024 (11)	-0.0048 (12)
O7	0.0107 (13)	0.0149 (13)	0.0153 (14)	-0.0019 (11)	-0.0009 (10)	0.0014 (12)
O8	0.0129 (13)	0.0119 (13)	0.0153 (15)	0.0000 (10)	-0.0011 (10)	0.0032 (11)
O9	0.0163 (17)	0.0104 (13)	0.0205 (18)	-0.0026 (11)	-0.0022 (13)	0.0036 (12)
O10	0.0089 (13)	0.0241 (16)	0.0160 (15)	0.0029 (12)	-0.0005 (10)	-0.0028 (12)
O11	0.0167 (14)	0.0088 (13)	0.0104 (14)	-0.0014 (11)	-0.0024 (11)	0.0026 (11)
O12	0.0115 (17)	0.0143 (16)	0.015 (2)	0.0013 (9)	0.0053 (12)	0.0003 (10)
O1W	0.0126 (13)	0.0131 (14)	0.0290 (17)	-0.0034 (11)	0.0055 (12)	-0.0034 (12)

O2W	0.0139 (14)	0.0141 (13)	0.0190 (15)	0.0006 (11)	0.0049 (11)	0.0029 (12)
O3W	0.0349 (17)	0.0137 (14)	0.0172 (15)	0.0030 (12)	0.0059 (13)	0.0009 (12)
O4W	0.0221 (18)	0.0371 (17)	0.0137 (17)	0.0168 (14)	-0.0068 (14)	-0.0093 (14)

Geometric parameters (Å, °)

Ce1—O10	2.449 (2)	S1—O2	1.437 (3)
Ce1—O7	2.465 (3)	S1—O5	1.462 (3)
Ce1—O12 ⁱ	2.476 (4)	S1—O11	1.498 (3)
Ce1—O11 ⁱⁱ	2.517 (3)	S1—O3	1.502 (3)
Ce1—O4W	2.524 (3)	S2—O8	1.460 (3)
Ce1—O3	2.547 (3)	S2—O10	1.463 (3)
Ce1—O3 ⁱ	2.621 (3)	S2—O6	1.465 (3)
Ce1—O1W	2.647 (3)	S2—O9	1.493 (3)
Ce1—O11	2.710 (3)	S3—O1	1.456 (3)
Ce1—S1	3.2607 (11)	S3—O4	1.463 (3)
Ce2—O1 ⁱⁱⁱ	2.354 (3)	S3—O7	1.466 (3)
Ce2—O4 ^{iv}	2.430 (3)	S3—O12	1.481 (3)
Ce2—O5 ⁱⁱⁱ	2.470 (3)	O1—Ce2 ^{vi}	2.354 (3)
Ce2—O6 ^v	2.489 (3)	O3—Ce1 ⁱ	2.621 (3)
Ce2—O3W	2.494 (3)	O4—Ce2 ^{iv}	2.430 (3)
Ce2—O2W	2.497 (3)	O5—Ce2 ^{vi}	2.470 (3)
Ce2—O9	2.529 (4)	O6—Ce2 ^v	2.489 (3)
Ce2—O8	2.659 (3)	O11—Ce1 ⁱⁱ	2.517 (3)
Ce2—S2	3.2143 (9)	O12—Ce1 ⁱ	2.476 (4)
O10—Ce1—O7	80.99 (9)	O4 ^{iv} —Ce2—O9	144.23 (11)
O10—Ce1—O12 ⁱ	135.57 (11)	O5 ⁱⁱⁱ —Ce2—O9	78.93 (11)
O7—Ce1—O12 ⁱ	136.10 (8)	O6 ^v —Ce2—O9	94.03 (10)
O10—Ce1—O11 ⁱⁱ	78.49 (9)	O3W—Ce2—O9	80.07 (9)
O7—Ce1—O11 ⁱⁱ	143.04 (9)	O2W—Ce2—O9	69.51 (10)
O12 ⁱ —Ce1—O11 ⁱⁱ	77.96 (8)	O1 ⁱⁱⁱ —Ce2—O8	75.74 (9)
O10—Ce1—O4W	67.91 (10)	O4 ^{iv} —Ce2—O8	149.39 (9)
O7—Ce1—O4W	115.31 (11)	O5 ⁱⁱⁱ —Ce2—O8	68.43 (9)
O12 ⁱ —Ce1—O4W	72.81 (13)	O6 ^v —Ce2—O8	76.73 (8)
O11 ⁱⁱ —Ce1—O4W	84.61 (10)	O3W—Ce2—O8	123.02 (9)
O10—Ce1—O3	150.11 (9)	O2W—Ce2—O8	110.19 (8)
O7—Ce1—O3	72.45 (8)	O9—Ce2—O8	53.57 (8)
O12 ⁱ —Ce1—O3	74.32 (10)	O1 ⁱⁱⁱ —Ce2—S2	102.43 (7)
O11 ⁱⁱ —Ce1—O3	115.47 (8)	O4 ^{iv} —Ce2—S2	160.40 (8)
O4W—Ce1—O3	136.36 (9)	O5 ⁱⁱⁱ —Ce2—S2	70.81 (7)
O10—Ce1—O3 ⁱ	113.98 (9)	O6 ^v —Ce2—S2	85.72 (6)
O7—Ce1—O3 ⁱ	69.68 (8)	O3W—Ce2—S2	101.58 (7)
O12 ⁱ —Ce1—O3 ⁱ	72.32 (8)	O2W—Ce2—S2	90.50 (6)
O11 ⁱⁱ —Ce1—O3 ⁱ	147.19 (9)	O9—Ce2—S2	26.89 (7)
O4W—Ce1—O3 ⁱ	73.70 (9)	O8—Ce2—S2	26.70 (6)
O3—Ce1—O3 ⁱ	69.49 (9)	O2—S1—O5	111.78 (19)
O10—Ce1—O1W	78.08 (9)	O2—S1—O11	112.17 (17)

O7—Ce1—O1W	67.17 (8)	O5—S1—O11	108.23 (17)
O12 ⁱ —Ce1—O1W	132.17 (10)	O2—S1—O3	110.58 (15)
O11 ⁱⁱ —Ce1—O1W	78.67 (9)	O5—S1—O3	109.98 (17)
O4W—Ce1—O1W	144.47 (9)	O11—S1—O3	103.78 (17)
O3—Ce1—O1W	79.12 (8)	O2—S1—Ce1	134.25 (15)
O3 ⁱ —Ce1—O1W	132.38 (8)	O5—S1—Ce1	113.83 (13)
O10—Ce1—O11	129.81 (9)	O11—S1—Ce1	55.52 (11)
O7—Ce1—O11	111.72 (8)	O3—S1—Ce1	49.18 (10)
O12 ⁱ —Ce1—O11	67.22 (10)	O8—S2—O10	112.44 (16)
O11 ⁱⁱ —Ce1—O11	62.40 (10)	O8—S2—O6	111.47 (16)
O4W—Ce1—O11	132.05 (10)	O10—S2—O6	109.46 (15)
O3—Ce1—O11	53.24 (9)	O8—S2—O9	104.86 (17)
O3 ⁱ —Ce1—O11	115.95 (7)	O10—S2—O9	109.15 (18)
O1W—Ce1—O11	65.00 (8)	O6—S2—O9	109.32 (19)
O10—Ce1—S1	144.70 (7)	O8—S2—Ce2	54.92 (10)
O7—Ce1—S1	89.84 (6)	O10—S2—Ce2	123.08 (11)
O12 ⁱ —Ce1—S1	71.67 (9)	O6—S2—Ce2	127.12 (11)
O11 ⁱⁱ —Ce1—S1	89.48 (6)	O9—S2—Ce2	50.02 (13)
O4W—Ce1—S1	144.45 (8)	O1—S3—O4	108.98 (17)
O3—Ce1—S1	26.51 (6)	O1—S3—O7	110.62 (16)
O3 ⁱ —Ce1—S1	94.06 (6)	O4—S3—O7	110.38 (16)
O1W—Ce1—S1	66.99 (6)	O1—S3—O12	108.69 (18)
O11—Ce1—S1	27.09 (6)	O4—S3—O12	108.21 (17)
O1 ⁱⁱⁱ —Ce2—O4 ^{iv}	81.47 (10)	O7—S3—O12	109.91 (19)
O1 ⁱⁱⁱ —Ce2—O5 ⁱⁱⁱ	82.75 (10)	S3—O1—Ce2 ^{vi}	159.40 (18)
O4 ^{iv} —Ce2—O5 ⁱⁱⁱ	128.77 (10)	S1—O3—Ce1	104.31 (13)
O1 ⁱⁱⁱ —Ce2—O6 ^v	72.44 (10)	S1—O3—Ce1 ⁱ	138.41 (14)
O4 ^{iv} —Ce2—O6 ^v	77.08 (10)	Ce1—O3—Ce1 ⁱ	110.51 (9)
O5 ⁱⁱⁱ —Ce2—O6 ^v	141.23 (10)	S3—O4—Ce2 ^{iv}	148.94 (18)
O1 ⁱⁱⁱ —Ce2—O3W	136.83 (10)	S1—O5—Ce2 ^{vi}	144.59 (18)
O4 ^{iv} —Ce2—O3W	87.59 (10)	S2—O6—Ce2 ^v	140.98 (15)
O5 ⁱⁱⁱ —Ce2—O3W	72.09 (10)	S3—O7—Ce1	138.57 (15)
O6 ^v —Ce2—O3W	144.78 (10)	S2—O8—Ce2	98.38 (13)
O1 ⁱⁱⁱ —Ce2—O2W	139.13 (9)	S2—O9—Ce2	103.09 (16)
O4 ^{iv} —Ce2—O2W	74.93 (9)	S2—O10—Ce1	147.70 (16)
O5 ⁱⁱⁱ —Ce2—O2W	137.81 (9)	S1—O11—Ce1 ⁱⁱ	144.95 (16)
O6 ^v —Ce2—O2W	70.06 (9)	S1—O11—Ce1	97.39 (12)
O3W—Ce2—O2W	75.42 (9)	Ce1 ⁱⁱ —O11—Ce1	117.60 (10)
O1 ⁱⁱⁱ —Ce2—O9	129.31 (9)	S3—O12—Ce1 ⁱ	136.67 (15)

Symmetry codes: (i) $-x+1, -y, -z+2$; (ii) $-x+1, -y+1, -z+2$; (iii) $x-1/2, -y+1/2, z-1/2$; (iv) $-x, -y, -z+2$; (v) $-x, -y+1, -z+2$; (vi) $x+1/2, -y+1/2, z+1/2$.